

# Lecture 28: Process Topology and MPI

William Gropp

[www.cs.illinois.edu/~wgropp](http://www.cs.illinois.edu/~wgropp)



# Virtual and Physical Topologies

---

- A *virtual topology* represents the way that MPI processes communicate
  - ◆ Nearest neighbor exchange in a mesh
  - ◆ Recursive doubling in an all-to-all exchange
- A *physical topology* represents that connections between the cores, chips, and nodes in the hardware



# Virtual and Physical Topologies

---

- Issue is mapping of the virtual topology onto the physical topology
  - ◆ Hierarchical systems (e.g., nodes of chips of cores) makes this more complicated; no simple topology
- Questions to ask
  - ◆ Does it really matter what mapping is used?
  - ◆ How does one get a good mapping?
  - ◆ How bad can a bad mapping be?
  - ◆ What if the mapping is random?
- This lecture is about using MPI to work with virtual topologies and make it possible for the MPI implementation to provide a good mapping



# MPI's Topology Routines

---

- MPI provides routines to create new communicators that order the process ranks in a way that *may* be a better match for the *physical topology*
- Two types of virtual topology supported:
  - ◆ Cartesian (regular mesh)
  - ◆ Graph (several ways to define in MPI)
- Additional routines provide access to the defined virtual topology
- (Virtual) topologies are properties of a communicator
  - ◆ Topology routines all create a *new* communicator with properties of the specified virtual topology



# MPI Cartesian Topology

---

- Create a new virtual topology using
  - ◆ `MPI_Cart_create`
- Determine “good” sizes of mesh with
  - ◆ `MPI_Dims_create`



# MPI\_Cart\_create

---

- `MPI_Cart_create(MPI_Comm oldcomm, int ndim, int dims[], int qperiodic[], int qreorder, MPI_Comm *newcomm)`
  - ◆ Creates a new communicator **newcomm** from **oldcomm**, that represents an **ndim** dimensional mesh with sizes **dims**. The mesh is periodic in coordinate direction *i* if **qperiodic[i]** is true. The ranks in the new communicator are reordered (to better match the physical topology) if **qreorder** is true



# MPI\_Dims\_create

---

- `MPI_Dims_create(int nnodes, int ndim, int dims[])`
- Fill in the **dims** array such that the product of **dims[i]** for  $i=0$  to **ndim-1** equals **nnodes**.
- Any value of **dims[i]** that is 0 on input will be replaced; values that are  $> 0$  will not be changed



# MPI\_Cart\_create Example

---

- ```
int periods[3] = {1,1,1};  
int dims[3] = {0,0,0}, wsize;  
MPI_Comm cartcomm;  
  
MPI_Comm_size(MPI_COMM_WORLD, &wsize);  
MPI_Dims_create(wsize, 3, dims);  
MPI_Cart_create(MPI_COMM_WORLD, 3, dims,  
                periods, 1, &cartcomm);
```
- Creates a new communicator **cartcomm** that *may* be efficiently mapped to the physical topology



# Information About a Cartesian Topology

---

- MPI\_Cartdim\_get
  - ◆ Dimension of Cartesian mesh (**ndim**)
- MPI\_Cart\_get
  - ◆ Size of dimensions (**dims**), periodic dimensions (**qperiodic**), coordinates of calling process in mesh



# Determine Neighbor Ranks

---

- Can be computed from rank (in the cartcomm), dims, and periods, since ordering defined in MPI
  - ◆ See Section 7.5 in MPI-3 Standard
- Easier to use either
  - ◆ MPI\_Cart\_coords, MPI\_Cart\_rank
  - ◆ MPI\_Cart\_shift



# MPI\_Cart\_shift

---

- `MPI_Cart_shift(MPI_Comm comm, int direction, int disp, int *rank_source, int *rank_dest)`
- Returns the ranks of the processes that are a shift of **disp** steps in coordinate **direction**
- Useful for nearest neighbor communication in the coordinate directions
  - ◆ Use `MPI_Cart_coords`, `MPI_Cart_rank` for more general patterns



# MPI Graph Topology

---

- MPI provides routines to specify a general graph virtual topology
  - ◆ Graph vertices represent MPI processes (usually one per process)
  - ◆ Graph edges indicate important connections (e.g., nontrivial communication between the connected processes)
  - ◆ Edge weights provide more information (e.g., amount of communication)



# MPI\_Dist\_graph\_create\_adjacent

---

- MPI\_Dist\_graph\_create\_adjacent(MPI\_Comm oldcomm, int indegree, int sources[], int sourceweights[], int outdegree, int dests[], int destweights[], MPI\_Info info, int qreorder, MPI\_Comm \*newcomm)
- Describe *only* the graph vertex corresponding to the calling process
  - ◆ Hence “Dist\_graph” – distributed description of graph
- Graph is directed – separate in and out edges
- **info** allows additional, implementation-specific information
- **qreorder** if true lets MPI implementation reorder ranks for a better mapping to physical topology
- **MPI\_UNWEIGHTED** may be used for weights *arrays*



# Other Graph Routines

---

- MPI\_Dist\_graph\_create
  - ◆ More general, allows multiple graph vertices per process
- Information on graph
  - ◆ MPI\_Dist\_graph\_neighbors\_count, MPI\_Dist\_graph\_neighbors



# Some Results (Good and Bad)

---

- A common virtual topology is *nearest neighbor in a mesh*
  - ◆ Matrix computations
  - ◆ PDE Simulations on regular computational grids
- Many Large Scale Systems use a mesh as the physical topology
  - ◆ IBM Blue Gene series; Cray through XE6/XK7
- Performance can depend on how well the virtual topology is mapped onto the physical topology



# Why Mesh Networks?

---

- Pros:
  - ◆ Scaling cost of adding a node is constant
  - ◆ Nearest neighbor bandwidth proportional to the number of nodes (thus scales perfectly as well)
  - ◆ Cabling relatively simple
- Cons:
  - ◆ Bisection bandwidth does *not* scale with network size
    - For 3D mesh, scales as  $n^2/n^3 = n^{2/3}$  for  $n \times n \times n$  mesh
  - ◆ Non-nearest neighbor communication suffers from contention



# Mesh Performance Limits

---

- What is the maximum aggregate bandwidth of an  $n \times n \times n$  mesh, assuming:
  - ◆ Each interior node sends at bandwidth  $L$  to each of its 6 neighbors ( $\pm x, \pm y, \pm z$  direction)
  - ◆ Edge nodes send to their immediate neighbors
- What is the bisection bandwidth of this network (simple cut along any coordinate plane)?



# Mesh Performance

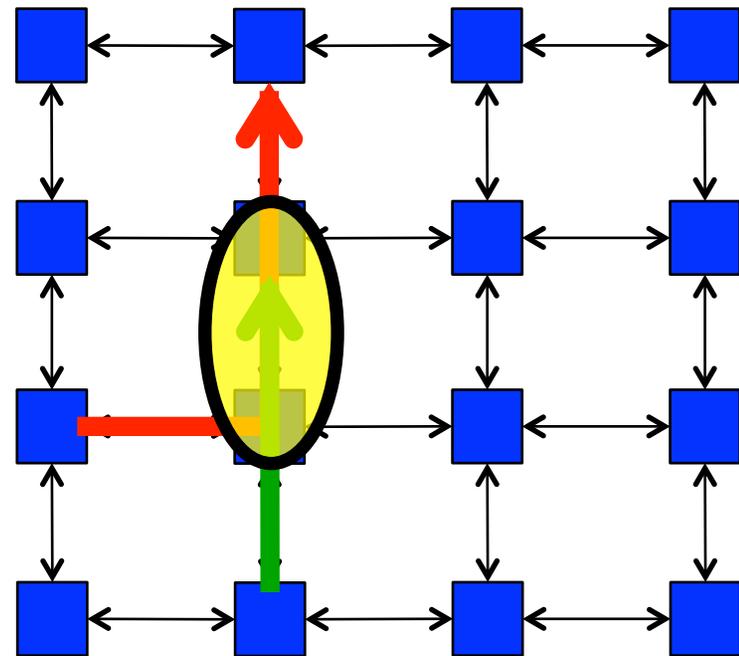
---

- Aggregate bandwidth
  - ◆ Simple, overestimate:  $n^3$  nodes \* 6 links/node \* L bytes/sec/link =  $6Ln^3$  bytes/sec
  - ◆ More accurate
    - $6L(n-2)^3 + 6(n-2)^25L + 12(n-2)4L + 8(1)3L$
    - i.e., Interior + 6 faces + 12 edges + 8 corners
- Bisection Bandwidth
  - ◆  $Ln^2$
- Note: Nearest neighbor bandwidth is more than n times bisection bandwidth
- For  $n=24$ ,  $L = 2\text{GB/sec}$ 
  - ◆ Neighbor =  $L*79488 = 159\text{ TB/sec}$
  - ◆ Bisection =  $L*576 = 1.2\text{TB/sec}$



# Communication Cost Includes More than Latency and Bandwidth

- Communication does not happen in isolation
- Effective bandwidth on shared link is  $\frac{1}{2}$  point-to-point bandwidth
- Real patterns can involve many more (integer factors)
- Loosely synchronous algorithms ensure communication cost is worst case



# Halo Exchange on BG/Q and Cray XE6

- 2048 doubles to each neighbor
- Rate is MB/sec (for all tables)

| <b>BG/Q</b> | <b>8 Neighbors</b> |             |
|-------------|--------------------|-------------|
|             | Irecv/Send         | Irecv/Isend |
| World       | 662                | 1167        |
| Even/Odd    | 711                | 1452        |
| 1 sender    |                    | 2873        |

| <b>Cray XE6</b> | <b>8 Neighbors</b> |             |
|-----------------|--------------------|-------------|
|                 | Irecv/Send         | Irecv/Isend |
| World           | 352                | 348         |
| Even/Odd        | 338                | 324         |
| 1 sender        |                    | 5507        |



# Discovering Performance Opportunities

- Lets look at a single process sending to its neighbors.
- Based on our performance model, we *expect* the rate to be roughly twice that for the halo (since this test is only sending, not sending and receiving)

| System | 4 neighbors |          | 8 Neighbors |          |
|--------|-------------|----------|-------------|----------|
|        |             | Periodic |             | Periodic |
| BG/L   | 488         | 490      | 389         | 389      |
| BG/P   | 1139        | 1136     | 892         | 892      |
| BG/Q   |             |          | 2873        |          |
| XT3    | 1005        | 1007     | 1053        | 1045     |
| XT4    | 1634        | 1620     | 1773        | 1770     |
| XE6    |             |          | 5507        |          |



# Discovering Performance Opportunities

- Ratios of a single sender to all processes sending (in rate)
- *Expect* a factor of roughly 2 (since processes must also receive)

| System | 4 neighbors |          | 8 Neighbors |          |
|--------|-------------|----------|-------------|----------|
|        |             | Periodic |             | Periodic |
| BG/L   | 2.24        |          | 2.01        |          |
| BG/P   | 3.8         |          | 2.2         |          |
| BG/Q   |             |          | 1.98        |          |
| XT3    | 7.5         | 8.1      | 9.08        | 9.41     |
| XT4    | 10.7        | 10.7     | 13.0        | 13.7     |
| XE6    |             |          | 15.6        | 15.9     |

- BG gives roughly double the halo rate. XTn and XE6 are much higher.
- It should be possible to improve the halo exchange on the XT by scheduling the communication
- Or improving the MPI implementation



# Limitations of MPI Process Topology Routines: Cartesian

---

- Dims\_create
  - ◆ Only for MPI\_COMM\_WORLD; if strictly implemented, nearly useless
  - ◆ Standard defines exact output, makes this a convenience routine for computing factors of an integer. This was the wrong definition
- Cart routines
  - ◆ Can be implemented, but can be nontrivial in non-mesh network



# Limitations of MPI Process Topology Routines: Graph

---

- Graph routines
  - ◆ Complex to implement. No good implementations in general use; research work limited
    - E.g., minimize “bandwidth” in the numerical sparse matrix sense of the connection graph. Does not minimize contention
- One-level
  - ◆ Doesn't address cores/chips, though `cart/graph_map` *could*



# MPI's Original Graph Routines

---

- MPI-1 and MPI-2 contained a different set of Graph topology routines
  - ◆ These required each process to provide the *entire* graph
  - ◆ Simplifies determination of virtual to physical topology mapping
  - ◆ Sensible when maximum number of processes was  $< 200$  (when MPI-1 created)
  - ◆ These routines are MPI\_Graph\_xxx
  - ◆ Do not use these in new codes



# Nonstandard Interfaces

---

- Many systems provide ways to
  - ◆ Control mapping of processes
  - ◆ Access the mapping
- Mapping on Job Startup
  - ◆ Sometimes called allocation mapping
  - ◆ Typically specified by environment variable or command line option



# Example: Blue Waters Allocation Mapping

---

- Environment variable
  - ◆ MPICH\_RANK\_REORDER\_METHOD
  - ◆ Values:
    - 0 = Round robin by *node*
    - 1 = Fill each node with processes before going to next node ("SMP ordering")
    - 2 = Folded by node (0,1,2,...,q,q,q-1,...,0)
    - 3 = Read from file named MPICH\_RANK\_ORDER
- Mapping to cores within node controlled by `-cc` and `-d` options to `aprun`
- <https://bluewaters.ncsa.illinois.edu/topology-considerations>



# Example Blue Gene/Q Allocation Mapping

---

- Option to runjob:
  - ◆ --mapping ABCDET
  - ◆ where order of letters indicates which torus coordinate (A-E) or process on node (T) increments (starting from the *right*)
  - ◆ Mapping with a file also possible
- <http://www.redbooks.ibm.com/redbooks/pdfs/sg247948.pdf>



# Mapping at Runtime

---

- Also known as Rank Reordering
- Create a new communicator that gives each MPI process a new rank to achieve a “better” mapping from virtual to physical topology
  - ◆ This is what the MPI Topology routines do
- Requires access to the physical topology
  - ◆ No standard method, but many systems provide an API
  - ◆ Clusters may provide hwloc

<http://www.open-mpi.org/projects/hwloc/>



# Access to Mesh Topology

---

- Simple routines available for Blue Waters (Cray systems with Gemini interconnect) and IBM Blue Gene/Q
- Provides access to physical mesh coordinates as well as chip, core number within node
- Example of scalable access to regular network



# Access to Mesh Topology

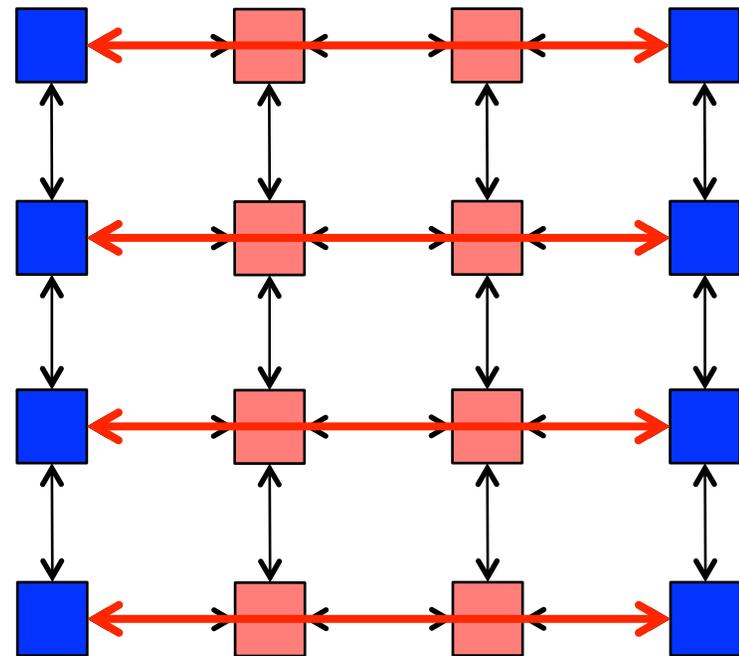
---

```
#include <stdio.h>
#include <string.h>
#include "mpi.h"
#include "topoinfo.h"
int main(int argc, char **argv)
{
    topoinfo_t *topoinfo;
    int wrank, verbose=0;
    char leader[10];
    MPI_Init(&argc,&argv);
    if (argv[1] && strcmp(argv[1],"-v") == 0) verbose = 1;
    MPI_Comm_rank(MPI_COMM_WORLD,&wrank);
    snprintf(leader,sizeof(leader),"%d:",wrank);
    topoInit(verbose,&topoinfo);
    topoPrint(stdout,leader,topoinfo);
    topoFinalize(&topoinfo);
    MPI_Finalize();
    return 0;
}
```



# Impact of Other Jobs

- Even with a perfect mapping, programs can suffer from *interference* with other jobs
- Can be reduced by *topology-aware* scheduling
- Layout of I/O nodes, adaptive routing can create contention even with topology-aware scheduling
- In this example, either the blue job or the pink job can communicate without contention, but together they share all of the “x” links in the pink job



# Readings

---

- Generic Topology Mapping Strategies for Large-scale Parallel Architectures, Hoefler and Snir  
<http://dx.doi.org/10.1145/1995896.1995909>
- Implementing the MPI Process Topology Mechanism, Traeff  
<http://www.computer.org/csdl/proceedings/sc/2002/1524/00/15240028-abs.html>
- Avoiding Hot Spots on Two-Level Direct Networks, Bhatele, Jain, Gropp, Kale  
<http://dl.acm.org/citation.cfm?doid=2063384.2063486>

